





# تعیین ضریب شکست غیرخطی مرتبه پنجم با استفاده از روش روبش Z کسوفی

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# Using Eclipsing Z-scan technique for determining the fifth order nonlinear refractive index

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Abstract- By replacing the aperture in the closed aperture (CA) Z-scan with an opaque disk, the modified version of Zscan namely the eclipsing Z-scan (EZ-scan) significantly enhances the peak-valley transmittance difference yielding a much greater measurement sensitivity than that observed with CA Z-scan at the similar conditions. This paper introduces the EZ-scan technique as a highly effective method for determining the fifth-order nonlinear (NL) refractive index of materials. The study highlights the higher sensitivity of the EZ-scan method for precise measurements and compares the sensitivity of CA Z-scan and EZ-scan. While an analytical relation for normalized transmittance can be derived for CA Z-scan, this is not feasible for the EZ-scan technique. Instead, an empirical relationship is proposed to determine the fifthorder NL refractive index from EZ-scan measurements. The proposed relation links the peak-valley transmittance difference, the fifth-order NL phase shift, and the disk obscureness, demonstrating that increased disk diameter improves sensitivity. This advancement provides a valuable tool for researchers in NL optics to determine the fifth order NL refractive index easily and precisely once the normalized transmittance of the EZ-scan is measured.

Keywords: Z-scan technique, Eclipsing Z-scan, Nonlinear optical properties, Nonlinear refractive index







# 1. Introduction

The nonlinear (NL) refractive index is an intensitydependent property of materials that causes a change in the refractive index due to intense light-matter interaction. This variation in refractive index can give rise to various phenomena, including self-phase modulation, cross-phase modulation, self-focusing, and self-defocusing, each of which holds significant practical relevance. These NL optical effects have enabled advancements in applications such as optical limiting and all-optical switching, a key component in photonic communication systems and signal processing [1].

Among various methods proposed for determining the NL refractive index, the Z-scan technique stands out due to its simplicity and high precision, making it a widely preferred approach in NL optical studies [2, 3]. In the closed aperture (CA) Z-scan version the sample is scanned along the propagation direction of a tightly focused laser beam while the power transmitted through a small aperture placed after the sample is measured as a function of the sample position. The resulting signal typically exhibits a characteristic valley-peak pattern for a positive NL refractive index or a peak-valley sequence for a negative NL refractive index.

In the eclipsing Z-scan (EZ-scan) technique, the aperture is replaced by an opaque disk, and the power transmitted around the disk is measured as a function of the sample position [4-6]. Since the intensity of a Gaussian beam decreases away from its center, changes in power transmitted around the disk are highly sensitive to variations in the beam size. Consequently, the sensitivity of the EZ-scan technique is much greater than that of the CA Z-scan method [7].

In this work, an empirical relationship is proposed to determine the fifth-order NL refractive index by measuring the maximum and minimum transmittance values of the EZ-scan signal.

## 2. Theory of Z-scan

In the Z-scan technique, the NL sample acts as a diffractive plane. Consequently, the electric field distribution on a plane positioned sufficiently far from the sample can be determined using the Fraunhofer diffraction integral.

$$E_a(z,r) = \frac{1}{i\,\lambda d} \int_0^\infty J_0(\frac{knr'}{d}) E_e(z,r') 2\pi r' dr'$$
(5)

where  $E_e = E_{in} \exp(i \Delta \Phi)$  is the electric field on the exit surface of the sample,  $E_{in}$  is the electric field incident on sample,  $\Delta \Phi = kL \Delta n$  is the NL phase change along the sample,  $k = 2\pi/\lambda$  is the wavenumber,

 $\lambda$  is the laser wavelength, L is the sample thickness,  $\Delta n = n_2 I$  with  $n_2$  the third order NL refractive index or  $\Delta n = n_4 I^2$  with  $n_4$  the fifth order NL refractive index and I is the intensity.

The normalized transmittance through an aperture can then be defined as

$$T(z) = \frac{\int_{0}^{r_{a}} \left| E(r, z, \Delta \Phi) \right|^{2} r dr}{\int_{0}^{r_{a}} \left| E(r, z, \Delta \Phi = 0) \right|^{2} r dr}$$
(6)

where  $r_a$  is the aperture radius.

Similar to Eq. (2), the normalized transmittance for EZscan can be defined by integrating the intensity from the edge of the obscuring disk to infinity.

$$T(z) = \frac{\int_{r_d}^{\infty} \left| E(r, z, \Delta \Phi) \right|^2 r dr}{\int_{r_a}^{\infty} \left| E(r, z, \Delta \Phi = 0) \right|^2 r dr}$$
(7)

where  $r_d$  is the disk radius.

Employing Eqs. (6) and (7), the normalized transmittance is obtained for CA Z-scan and EZ-scan by substituting  $\Delta \Phi = kLn_2I$  in the case of third order nonlinearity or  $\Delta \Phi = kLn_4I^2$  in the case of fifth order nonlinearity.

Further calculations reveal a relationship between the NL phase change and the peak-valley transmittance difference in the Z-scan technique when using a Gaussian laser beam. In CA Z-scan, for a medium with third-order

nonlinearity  

$$\Delta T_{pv} = 0.406(1 - S_a)^{0.25} |\Delta \Phi_0|$$
and for a  
medium with fifth order nonlinearity  

$$\Delta T_{pv} = 0.21(1 - S_a)^{0.25} |\Delta \Phi_0|$$
where  

$$\Delta T_{mv} = T_{mv} - T_{mv}$$

 $\sum_{pv} P_{max} P_{min}$  denotes the peak-valley transmittance difference,  $S_a$  is the aperture transmittance given by  $S_a = \left[1 - \exp(-2w^2/r_a^2)\right]$  and W is the beam radius on the aperture plane.

In the EZ-scan performed for a medium with third order nonlinearity  $\Delta T_{pv} = 0.68(1-S_d)^{-0.44} |\Delta \Phi_0|$  where  $S_d = [1 - \exp(-2w^2/r_d^2)]$  denotes the disk obscureness.





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## 3. Results and discussions

Figure 1 compares the normalized transmittance measured by CA Z-scan and EZ-scan for a fifth-order NL phase change of 0.1 rad. The red curve represents the CA Z-scan signal with a small aperture transmitting 1% of the laser beam power, while the blue curve corresponds to the EZ-scan signal, where a large opaque disk blocks 99% of the beam power.



Fig. 1. Normalized Transmittance assuming a fifth order phase change of 0.1 rad. Red curve indicates the CA Z-scan signal and blue curve represents the EZ-scan signal.

As shown, the peak-valley transmittance difference in EZ-scan is approximately 25 times greater than that in CA Z-scan, resulting in significantly higher sensitivity for determining the NL refractive index. To establish an empirical relationship between the peak-valley transmittance difference, fifth-order NL phase change, and disk obscureness, the normalized transmittance was computed using Eq. (3) for varying phase changes and disk obscureness. Figure 2 illustrates the EZ-scan normalized transmittance for a fifth-order NL phase change of 0.15 rad, considering disk obscureness of S=0.95, 0.98, 0.99 and 0.995. The results demonstrate that as the disk obscureness more pronounced, thereby improving the sensitivity of the technique.



Fig. 2. EZ-scan normalized transmittance for different disk obscureness.

Figure 3 illustrates the EZ-scan normalized transmittance for varying fifth order NL phase change considering a large opaque disk blocking 99% of the laser beam power. As anticipated, the peak-valley transmittance difference increases with increasing the fifth order NL phase change.



Fig. 3. EZ-scan normalized transmittance for different fifth order NL phase change.

Fig. 4 exhibits the Peak-valley transmittance different versus disk obscureness assuming a fifth order NL phase change of 0.05 rad.



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Fig. 4. Peak-valley transmittance different versus disk obscureness.

The circles in Fig. 4 show the calculated data points and the solid blue line represents the fitted curve described by  $\Delta T_{pv} = 0.4(1-S)^{-0.52} \left| \Delta \Phi_0 \right|$ 

Further investigation reveals that the proposed empirical relation remains valid for larger NL phase change up to approximately 0.2 rad for large disk obscureness in the range of  $0.9 \le S_d \le 0.995$ .

Fig. 5 illustrates the Peak-valley transmittance different versus NL phase change for different disk obscureness of 0.98, 0.99 and 0.995. The straight lines represent the linear fit given by the proposed relation  $\Delta T_{pv} = 0.4(1-S)^{-0.52} |\Delta \Phi_0|$  confirming its validity within the range of investigation.



*Fig. 5. Peak-valley transmittance different versus fifth order NL phase change for different disk obscureness.* 

# 4. Conclusion

The normalized transmittance for two versions of Zscan, namely CA Z-scan and EZ-scan, was calculated and compared for fifth-order nonlinearity. The results indicate that the measurement sensitivity of EZ-scan is at least 25 times greater than that of CA Z-scan. While an analytical relation for the normalized transmittance as a function of sample position can be derived for CA Zscan, this is not possible for EZ-scan. Therefore, we proposed an empirical relation that enables the determination of the fifth-order NL refractive index once the normalized transmittance for EZ-scan with a known disk radius is measured.

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